A New Three-Phase Power-Factor Correction (PFC) Scheme Using Two Single-Phase PFC Modules

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Abstract—In this paper, a new three-phase power-factor correction (PFC) scheme is proposed using two single-phase PFC modules. In this approach, the "three" phase input is first transformed to "two" phase by means of a 0.14-pu-rated autotransformer. Two standard single-phase PFC modules are then employed to process the "two" phase power to dc output. Split inductors and diodes are employed to limit interaction between the two PFC stages. Due to cascade operation of two PFC stages, low-frequency (120 Hz) ripple in the dc-link capacitor is cancelled. Detailed analysis and simulation results are presented. A 220-V 1.5-kVA design example along with experimental results is shown.

Index Terms—Harmonics, power-factor correction, power quality.

I. INTRODUCTION

■ HREE-PHASE switch-mode power supplies (SMPSs) employing diode-rectifier-type utility interface are widely used in telecommunications, data processing, and other industrial systems [1], [2]. The diode-rectifier-type utility interface generates lower order harmonics of the order $6k \pm 1$, i.e., 5, 7, 11, 13, etc. IEC 61 000-3-4 and IEEE 519-1992 detail acceptable limits [3], [4] of such nonlinear loads. Several approaches have been studied and summarized in [5]-[8] to improve the total harmonic distortion (THD). They are broadly categorized into two groups: 1) rectifier circuitry capable of producing low level of harmonic content or 2) conventional rectifier circuitry with additional filter. Three single-phase power-factor correction (PFC) stages for a three-phase system, a single-switch PFC with discontinuous mode (DCM) control, and a six-switch PWM rectifier can be considered in the first category. A single-switch PFC with DCM control suffers from high switch current rating and high electromagnetic interference (EMI) [6], [7]. A pulsewidth modulation (PWM) rectifier needs complicated measurements and feedback control [5].

This paper proposes a new three-phase PFC scheme using two standard single-phase PFC modules. "Two" phase is produced by means of a 0.14-pu-rated autotransformer from a "three" phase input. Two standard single-phase PFC modules are em-

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Fig. 1. Proposed three-phase PFC scheme using two single-phase PFC modules. (a) Topology of the proposed approach. (b) Vector diagram of the two phase.



Fig. 2. Input voltage waveforms and the interval $\pi/18 < \omega t < \pi/2$ considered in analysis. (a) Phase voltage. (b) Input voltages at each PFC.

ployed, one on each phase to process the power. Split inductors and diodes are used to limit interaction between the two PFC stages. The outputs of the two PFC modules are connected



Fig. 3. Equivalent circuits at each switching period. (a) Equivalent circuit in which S_1 is on while S_2 is on. (b) Equivalent circuit in which S_1 is on while S_2 is off. (c) Equivalent circuit in which S_1 is off while S_2 is on. (d) Equivalent circuit in which S_1 and S_2 are off.

to the common dc output. Due to cascade operation of the two PFC stages, low-frequency (120 Hz) ripple components in the dc-link capacitor cancel each other. The advantages of the proposed scheme are as follows.

- The proposed approach is modular and employs two standard single-phase PFC modules. Input current waveforms are nearly sinusoidal at unity power factor and are in compliance with IEEE 519, IEC 1000-3, and IEC-6000-3-2 limits.
- In this scheme, the second-order harmonic current component in the dc-link capacitor is cancelled. This significantly reduces capacitor heating and improves its operating life.
- The voltampere (VA) rating of the autotransformer employed is low.
- The dc output is regulated and is immune to voltage sags and other power quality disturbances.

II. PROPOSED SYSTEM

Fig. 1(a) shows the topology of the proposed approach. The three-phase input v_a , v_b , and v_c (120° phase shift) is first transformed to two phase v_{ab} and v_{ck} (90° phase shift) by means

of a center-tapped autotransformer. From the vector diagram in Fig. 1(b), it is clear that voltage v_{ab} and v_{ck} are 90° apart.

Two single-phase boost PFC stages are connected to the "two" phase voltages v_{ab} and v_{ck} , as shown in Fig. 1(a). Single-phase PFC module 1 consists of a bridge rectifier, inductors L_{1f} and L_{1b} , and diodes D_{1f} and D_{1b} . Single-phase PFC module 2 consists of a bridge rectifier, inductors L_{2f} and L_{2b} , and diodes D_{2f} and D_{2b} . Split inductors and diodes are employed at the two PFC stages to limit interaction between the two when the output stages are combined [8].

Although $|V_{ab}| \neq |V_{ck}|$ [Fig. 1(b)], the two boost PFC stages are suitably controlled with different gains to supply one-half of the output power. This feature enables cancellation of low-frequency second-order harmonic current component in the capacitor.

A. Analysis

Fig. 2(a) shows the phase voltages. Single-phase PFC module 1 sees the voltage v_{ab} as in Fig. 2(b) and single-phase PFC module 2 sees the voltage v_{ck} in Fig. 2(b) via the autotransformer. Fig. 3 shows the possible equivalent circuits from the input to the output.

In the interval of $\pi/18 < \omega t < \pi/2$ (gray area in Fig. 2), the rectified output has the following relationship:

$$|v_{ab}| > |v_{ck}| \tag{1}$$

$$d_{ab} = 1 - \frac{|v_{ab}|}{V_o} \tag{2.a}$$

$$d_{ck} = 1 - \frac{|v_{ck}|}{V_o} \tag{2.b}$$

where d_{ab} and d_{ck} are the duty cycles of each converter.

When both S_1 and S_2 switches are on, there is no current path to the output and the two single-phase PFC modules work independently as in Fig. 3(a). Also, when one of the switches, i.e., S_1 or S_2 is off [the equivalent circuit is shown in Fig. 3(b) and (c)], the PFC modules operate independently. However, when both switches are off the two PFC modules are simultaneously connected to the output.

The equivalent circuit for this condition is shown in Fig. 3(d). For this equivalent circuit,

$$v_{ab} - L_{1f} \frac{di_{1f}}{dt} - V_o - L_{1b} \frac{di_{1b}}{dt} = 0$$
 (3.a)

$$v_{ck} - L_{2f} \frac{di_{2f}}{dt} - V_o - L_{2b} \frac{di_{2b}}{dt} = 0$$
(3.b)

$$-\frac{v_{ab}}{2} + L_{1b} \frac{di_{1b}}{dt} - L_{2b} \frac{di_{2b}}{dt} = 0$$
(3.c)

$$i_{1f} + i_{2f} - i_{1b} - i_{2b} = 0.$$
 (3.d)

Assuming that $L = L_{1f} = L_{1b} = L_{2f} = L_{2b}$, the inductor current can be derived from (3.a)–(3.d).

$$\frac{di_{1f}}{dt} = \left(|v_{ab}| - \frac{|v_{ck}|}{2} - V_o \right) \frac{1}{2L}$$
(4.a)
$$\frac{di_{1b}}{dt} = \left(|v_{ab}| + \frac{|v_{ck}|}{2} - V_o \right) \frac{1}{2L}$$
(4.b)

$$\frac{di_{2f}}{dt} = \left(|v_{ck}| + \frac{|v_{ck}|}{2} - V_o \right) \frac{1}{2L} \\
= \left(\frac{3|v_{ck}|}{2} - V_o \right) \frac{1}{2L}$$
(4.c)

$$\begin{aligned} \frac{di_{2b}}{dt} &= \left(|v_{ck}| - \frac{|v_{ck}|}{2} - V_o \right) \frac{1}{2L} \\ &= \left(\frac{|v_{ck}|}{2} - V_o \right) \frac{1}{2L}. \end{aligned}$$
(4.d)

Fig. 4 shows the inductor current waveforms for a switching period in the interval, S_1S_2 on, S_1 off S_2 on, S_1S_2 off. From this figure, it is clear that the two PFC stages interact during the S_1S_2 off region. To minimize this effect, a split inductor configuration is chosen in each PFC stage. By proper design of L_{1f} , L_{1b} , L_{2f} , and L_{2b} , the interaction can be kept to a minimum and the input current quality is not affected.

B. Staggered PWM

To overcome the interaction between phases, staggered PWM is used. The two single-phase PFC modules can work independently by avoiding the Fig. 3(d) period. If 180° phase-shifted



Fig. 4. Inductor current waveforms for a switching period.



Fig. 6. Input voltage versus duty ratio.

PWM carrier signals are used and the duty ratio is higher than 0.5 when the two input voltages are the same, the interaction is virtually eliminated. Fig. 5 shows the gating signals of both switches.

The input voltages and the duty ratio have the relationship as in Fig. 6. Since the input voltages become the same at $\pi/18$, minimum output voltage for the staggered PWM is calculated as

$$V_o \ge \frac{1}{1 - D} V_{\rm in} \left(\frac{\pi}{18}\right) \tag{5.a}$$

or

$$V_o \ge 1.85 V_{LL}$$
. (5.b)



Fig. 7. Control block diagram of the system.



Fig. 8. Power-flow diagram of the proposed system.

C. Control Scheme

Fig. 7 shows the control block for the system. $V_{\rm FF,i}$ is dc voltage proportional to the rectified voltage $V_{\rm rec, i}$. The rectified input current $I_{\rm rec, i}$ and the current reference $I_{\rm ref, i}$ can be represented as

$$I_{\text{ref},i} = K_s K_M \frac{V_{\text{rec},i}}{K_{\text{in}}} \cdot \frac{1}{K_{\text{FF}}^2 V_{\text{rec},i}^2} V_{\text{EA}}$$
(7)

where

- K_s PFC power stage gain;
- K_M multiplier gain;
- $K_{\rm FF}$ feedforward gain;
- Kin waveform input gain;
- $V_{\rm EA}$ voltage error amplifier output.

$$I_{\text{rec},i} = K_s I_{\text{ref},i}, \qquad i = 1, 2$$
 (6)



Fig. 9. Power processed at each PFC.

From (6) and (7), the rectified current $I_{\text{rec}, i}$ is proportional to the reciprocal of $V_{\text{rec}, i}$. Therefore, the input power P_i is

$$P_i = V_{\text{rec}, i} I_{\text{rec}, i} = \frac{K_s K_M}{K_{\text{in}} K_{\text{FF}}^2} V_{\text{EA}}, \qquad i = 1, 2.$$
 (8)

Each PFC module can carry the same amount of power simply by sharing the same voltage error amplifier output.

D. Power Flow and Autotransformer Rating

Fig. 8 shows the power-flow diagram in the proposed approach. K_1 and K_2 represent the boost block. F_o is the output filter and T the autotransformer. Each boost PFC module supplies the same power (P_1 and P_2), which flows to the dc side as dc power ($P_{1,o}$ and $P_{2,o}$) and to the filter F_o as the power oscillating at twice the line frequency ($P_{1,2f}$ and $P_{2,2f}$).

The relationship between the sources and each single-phase PFC module is

$$P_a + P_b = P_1 + \frac{1}{3}P_2 \tag{9}$$
$$P_a - \frac{2}{3}P_a \tag{10}$$

$$P_c = \frac{1}{3} P_2.$$
 (10)
but voltages v_{ch} and v_{ch} of the two single-

Since the two input voltages v_{ab} and v_{ck} of the two singlephase PFC modules are in right angle, the second-order harmonic power components are cancelled each other. Therefore, the output filter capacitor F_o sees only switching frequency component (P_F).

The power processed in each module is shown in Fig. 9. The solid line represents output power. Dashed lines are the power via the single-phase PFC module 1 (P_1) and the power via the single-phase PFC module 2 (P_2).

The rms currents through the single-phase PFC module 1 and the single-phase PFC module 2 can be calculated as

$$P_1 = \frac{1}{2} P_{\rm in} \tag{11}$$

$$V_{LL}I_1 = \frac{1}{2} \left(\sqrt{3} V_{LL}I_a\right) \tag{12}$$

or

$$I_1 = \frac{\sqrt{3}}{2} I_a = 0.8660 I_a. \tag{13}$$

From the vector diagram,

$$V_2 = \frac{\sqrt{3}}{2} V_{LL}.$$
 (14)



Fig. 10. Simulated waveforms. (a) Input current waveforms at each PFC. (b) Input line current I_a , I_b , and I_c .

Since the two PFC modules process the same power,

$$P_2 = \frac{1}{2} P_{\rm in}$$
 (15)

or

$$\left(\frac{\sqrt{3}}{2}V_{LL}\right)I_2 = \frac{1}{2}\left(\sqrt{3}V_{LL}I_a\right).$$
(16)

Therefore,

$$I_2 = I_a. \tag{17}$$

With high power factor, the voltage and current waveforms are in phase by definition. Thus, the instantaneous input powers of the single-phase PFC module 1 $(p_{\text{in},1})$ and the single-phase PFC module 2 $(p_{\text{in},2})$ are calculated as the following:

$$p_{\text{in},1} = \left(\sqrt{2} V_{LL} \sin \omega t\right) \left(\sqrt{2} \frac{\sqrt{3}}{2} I_a \sin \omega t\right)$$
$$= \sqrt{3} V_{LL} I_a \sin^2 \omega t$$
$$= \frac{\sqrt{3}}{2} V_{LL} I_a (1 - \cos 2\omega t) \qquad (18)$$
$$p_{\text{in},2} = \left(\sqrt{2} V_{LL} \cos \omega t\right) \left(\sqrt{2} \frac{\sqrt{3}}{2} I_a \cos \omega t\right)$$
$$= \sqrt{3} V_{LL} I_a \cos^2 \omega t$$
$$= \frac{\sqrt{3}}{2} V_{LL} I_a (1 + \cos 2\omega t). \qquad (19)$$

TABLE I	
(a) VA RATING OF THE AUTO-TRANSFORMER (rms VALUE) AND (b) OPERATING CONDITION

Auto-transformer		Expression	rms value
Primary(secondary) winding current	I _{ak}	0.5000 Ia	2.0 [A]
Primary(secondary) winding voltage	V _{ak}	$0.5000V_{LL}$	110 [V]
VA rating	VA _{TR}	0.1443 P _o	216.5 [VA]

(a)

750 [374]
/50[VA]
190 - 250 [V _{rms}]
165 – 217 [V _{rms}]
380 [V _{dc}]
60 [Hz]
20 [kHz]

(b)

The output capacitor is considered to be large enough to hold the dc-link voltage V_{dc} fairly constant. The power outputs to the output capacitor from each boost PFC ($p_{chg,1}$ and $p_{chg,2}$) are

$$p_{\rm chg,\,1} = V_{\rm dc} i_{\rm chg,\,1}.\tag{20}$$

Since $p_{\text{in},1} = p_{\text{chg},1}$,

$$i_{\text{chg},1} = p_{\text{chg},1}/V_{\text{dc}}$$
$$= \left\{ \frac{\sqrt{3}}{2} V_{LL} I_a (1 - \cos 2\omega t) \right\} / V_{\text{dc}}. \quad (21)$$

 $i_{\mathrm{chg},\,2}$ can be calculated by the same way

$$i_{\rm chg,\,2} = \left\{ \frac{\sqrt{3}}{2} V_{LL} I_a (1 + \cos 2\omega t) \right\} / V_{\rm dc}.$$
 (22)

Therefore, the current at the output capacitor i_{chg} can be calculated by adding these two current components

$$i_{\rm chg} = i_{\rm chg, 1} + i_{\rm chg, 2}$$
$$= \left(\sqrt{3} V_{LL} I_a\right) / V_{\rm dc}.$$
(23)

Equation (23) shows that there is only dc current component at the output capacitor.

The current fed through the center-tapped autotransformer by phases a and b returns through phase c. Therefore, the rms value of the winding current is half of I_c . The voltage across the end of the autotransformer is line-to-line voltage. The power handled by the autotransformer is

$$P_{TR} = \frac{1}{2} \left\{ \left(\frac{1}{2} V_{LL} \right) * \left(\frac{1}{2} I_a \right) * 2 \right\} = \frac{1}{4} V_{LL} I_a.$$
(24)

Then, the VA rating of the autotransformer is

$$VA_{TR} = \frac{P_{TR}}{P_{\rm in}} = \frac{\frac{1}{4}V_{LL}I_a}{\sqrt{3}V_{LL}I_a} = 0.1443.$$
 (25)

III. SIMULATION RESULTS

Fig. 10 shows the simulation result of the proposed system. A simple proportional plus integral (PI) controller is used for the inner current control loop. The voltage control loop feeds the current references of the two single-phase PFC modules forcing current sharing between them.

The amplitudes of input currents at each PFC [Fig. 10(a)] are different to carry the same power. The input line current waveforms are near sinusoidal [Fig. 10(b)], which demonstrates the proposed approach.

IV. DESIGN EXAMPLE

Table I summarizes the VA rating of the autotransformer and the operating condition of each PFC module. For an output power of 1.5 kVA, each PFC module supplies 750 VA. Design of each PFC modules follows the single-phase boost PFC operating in continuous conduction mode (CCM) [10]. Since the low-frequency power components cancel each other, the output capacitor handles only high-frequency ripple elements.

V. EXPERIMENTAL RESULTS

The proposed three-phase PFC rated at 220 V, 1.5 kVA (Fig. 1) has been implemented and the results are discussed in this section. Both PFC modules are controlled by Unitrode UC3854A controllers. Fig. 11(a) shows the input currents I_{a1} and I_c of each PFC which are 90° phase shifted and the amplitudes are different so that their respective output powers are equal. Fig. 11(b) shows the line currents I_a , I_b and I_c . They are nearly sinusoidal in shape. Fig. 11(c) and (d) shows the voltage V_{ab} and current I_{a1} ; V_{ck} and current I_c , respectively. It is clear from the figure that each PFC stage operates in CCM at unity power factor.

VI. CONCLUSION

In this paper, a new three-phase PFC scheme using two standard single-phase PFC modules has been presented. Each PFC module is rated for half the output power and operates in CCM with unity power factor. With staggered PWM, the



Fig. 11. Experimental results. (a) Current waveforms at each PFC (I_{a1} and I_c (2 A/div). (b) Line current waveforms (I_A , I_b , and I_c) (2 A/div). (c) PFC 1 input (V_{ab} and I_{a1}) (5 A/div). (d) PFC 2 input (V_{ck} and I_c) (5 A/div).

interaction between PFC modules is virtually eliminated. The resulting input line currents are nearly sinusoidal in shape. The experimental result from a laboratory prototype demonstrates the performance of the proposed system.

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