

## 1 Off-time:

$$V_{start} \approx 0.6$$

Assuming  $R_1 \gg R_3$  and  $V_{out} \gg I_{max}R_{14}$

$$V_{stop} = V_{in} \frac{R_6}{R_6 + R_2}$$

### 1.1 For Design 1

(with off time set by simple RC network)

$$t_{off} = R_1 C_1 \ln \left( \frac{V_{out} - V_{start}}{V_{out} - V_{stop}} \right)$$

linear approximation when  $V_{out} \gg V_{stop} - V_{start}$

$$t_{off} \approx R_1 C_1 \left( \frac{V_{stop} - V_{start}}{V_{out} - V_{stop}} \right)$$

### 1.2 For design 2

(with off time set by C and const I)

Assuming  $V_{out} - V_{in} \gg 0.6$

$$t_{off} = \frac{R_1 C_1}{V_{out} - V_{in}} (V_{stop} - V_{start})$$

## 2 Currents

### 2.1 Input and output current

$$I_{avg,in} = I_{max} - t_{off} \left( \frac{V_{out} - V_{in}}{2L_1} \right)$$

$$I_{avg,out} = \frac{V_{in}}{V_{out}} \left[ I_{max} - t_{off} \left( \frac{V_{out} - V_{in}}{2L_1} \right) \right]$$

### 2.2 Input current, design 1

Accurate result

$$I_{avg,in} = I_{max} - \frac{R_1 C_1 (V_{out} - V_{in})}{2L_1} \ln \left( \frac{V_{out} - V_{start}}{V_{out} - V_{stop}} \right)$$

aproximate result

$$I_{avg,in} \approx I_{max} - R_1 C_1 \frac{V_{stop} - V_{start}}{2L_1} \frac{V_{out} - V_{in}}{V_{out} - V_{stop}}$$

as  $V_{stop} \rightarrow V_{in}$  then

$$I_{avg,in} \approx I_{max} - R_1 C_1 \frac{V_{in} - V_{start}}{2L_1}$$

which is independent of  $V_{out}$

We could like therefore to make  $V_{start}$  high, possibly clamping it a fixed voltage below  $V_{in}$ , but this comes into conflict with the requirement for the time constant  $R_3 C_1$  to be low.



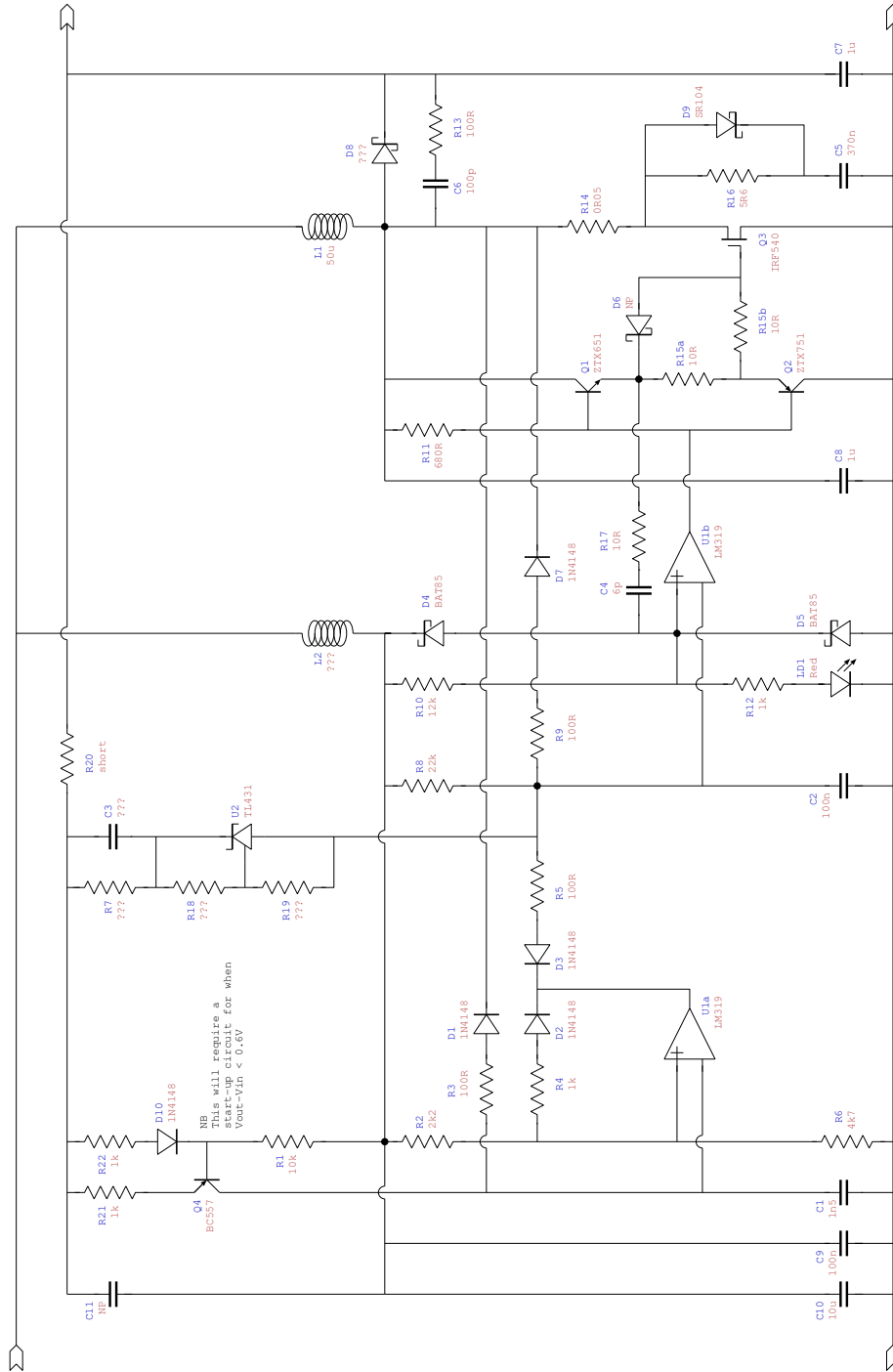


Figure 2: Design 2

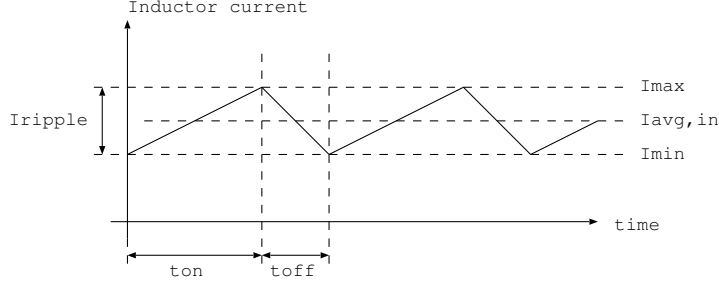


Figure 3: Inductor current

### 2.3 Input current, design 2

$$I_{avg,in} = I_{max} - \frac{R_1 C_1}{2L_1} (V_{stop} - V_{start})$$

If  $V_{start}$  is small,

$$I_{avg,in} = I_{max} - \frac{R_1 C_1 V_{in}}{2L_1} \frac{R_6}{R_6 + R_2}$$

Input current decreases with  $V_{in}$  but is independent of  $V_{out}$   
 replace  $R_6$  with constant-voltage to remove this dependence

## 3 Threshold

Let inputs to U1b be  $V_{comp+}$  and  $V_{comp-}$

$$V_{comp+} = \frac{V_{in} \frac{R_{12}}{R_{10}} + V_{LD1}}{\frac{R_{12}}{R_{10}} + 1}$$

$$V_{comp-} = \frac{I_{L1} R_{14} + V_{D7} + V_{in} \frac{L_1}{L_{stray,R14}} + V_{in} \frac{R_9}{R_8} + V_{out} \frac{R_9}{R_7} - V_{U2} \frac{R_9}{R_7}}{\frac{R_9}{R_7} + \frac{R_9}{R_8} + 1}$$

the term  $V_{in} \frac{L_1}{L_{stray,R14}}$  is valid only during the “on” period

When  $V_{comp-} = V_{comp+}$  then  $I_{L1} = I_{max}$

$$I_{max} = \frac{\left(\frac{R_9}{R_8} + \frac{R_9}{R_7} + 1\right) \left(V_{in} \frac{R_{12}}{R_{10}} + V_{LD1}\right)}{R_{14} \left(\frac{R_{12}}{R_{10}} + 1\right)} - \frac{V_{D7} + V_{in} \frac{L_1}{L_{stray,R14}} + V_{in} \frac{R_9}{R_8} + V_{out} \frac{R_9}{R_7}}{R_{14}} + \frac{V_{U2} R_9}{R_{14} R_7}$$

#### 3.0.1 Approximation

As an approximation, if  $V_{comp} \ll V_{in}$ , we can assume that all of  $V_{in}$  is dropped across  $R_{10}$  and  $R_8$  (terms in  $R_9$  and  $R_{12}$  disappear from the first half of above equation)

$$I_{max} \approx \frac{V_{in} \frac{R_{12}}{R_{10}} + V_{LD1}}{R_{14}} - \frac{V_{D7} + V_{in} \frac{L_1}{L_{stray,R14}} + V_{in} \frac{R_9}{R_8} + V_{out} \frac{R_9}{R_7}}{R_{14}} + \frac{V_{U2} R_9}{R_{14} R_7}$$

if  $\frac{R_{12}}{R_{10}} = \frac{R_9}{R_8} + \frac{L_1}{L_{stray,R14}}$  then  $I_{max}$  is independent of  $V_{in}$

$$I_{max} \approx \frac{V_{LD1}}{R_{14}} - \frac{V_{D7}}{R_{14}} + (V_{U2} - V_{out}) \frac{R_9}{R_7 R_{14}}$$

### 3.1 Current limit

When out of regulation (U2 not conducting) all terms in  $R_7$  become 0.

$$I_{max,limit} = \frac{\left(\frac{R_9}{R_8} + 1\right) \left(V_{in} \frac{R_{12}}{R_{10}} + V_{LD1}\right)}{R_{14} \left(\frac{R_{12}}{R_{10}} + 1\right)} - \frac{V_{D7} + V_{in} \frac{L_1}{L_{stray, R14}} + V_{in} \frac{R_9}{R_8}}{R_{14}}$$

$$I_{max,limit} \approx \frac{V_{LD1}}{R_{14}} - \frac{V_{D7}}{R_{14}}$$

#### 3.1.1 Design 1

Using the linear approximation of average current

$$I_{avg,in,limit} \approx \frac{V_{LD1}}{R_{14}} - \frac{V_{D7}}{R_{14}} - R_1 C_1 \left( \frac{V_{stop} - V_{start}}{2L_1} \frac{V_{out} - V_{in}}{V_{out} - V_{stop}} \right)$$

### 3.2 Voltage limit

$$V_{out,limit} \approx V_{U2} + \frac{R_7}{R_9} (V_{LD1} - V_{D7})$$

The difference  $V_{out,limit} - (V_{U2} + V_{LD1})$  represents the output sag from unloaded to full load