

a) Common Mode voltage gain: (single-ended)

$$A_{cm} = \frac{V_o}{V_{cm}} = \frac{V_{o2}}{V_{s1}} \bigg|_{V_{s2}=V_{s1}} = -g_{m2} R_{D2} [1 + g_{m1} R_s - g_{m1} R_s] \frac{1}{\Delta}$$

$$\left| A_{cm} = -\frac{g_m R_D}{1 + 2g_m R_s} = -\frac{1}{2} \frac{R_D}{R_s \left(1 + \frac{1}{2g_m R_s}\right)} \right| \quad \frac{-g_m R_D}{2R_s g_m + 1}$$

b) Differential Mode voltage gain: (single-ended)

$$A_d = \frac{V_o}{V_d} = \frac{V_{o2}}{V_{s1}} \bigg|_{V_{s2}=0} = g_{m1} R_s g_{m2} R_{D2} \frac{1}{\Delta}$$

$$\left| A_d \approx \frac{g_m R_s g_m R_D}{1 + 2g_m R_s} = \frac{1}{2} \frac{g_m R_D}{\left(1 + \frac{1}{2g_m R_s}\right)} \right|$$

c) Common Mode Rejection Ratio:

$$\left| CMRR = \frac{|A_d|}{|A_{cm}|} \approx g_m R_s \right|$$

Numerical Example

$$R_D = 39k\Omega$$

$$R_s = 18k\Omega$$

$$g_m = 4 \times 10^{-4} \frac{A}{V}$$

$\Rightarrow$

$$\left| \begin{array}{l} A_{cm} \approx -1.01 \\ A_d \approx 7.29 \\ CMRR \approx 7.2 \end{array} \right|$$

Conclusion: To improve both  $A_d$  and  $CMRR$  we have to replace  $R_D$  and  $R_s$  by current sources!  $\rightarrow$  active Loads